

7-2 Graphing Polynomial Functions

End Behavior

Using a graphing calculator find the end behavior of the following functions. Where do the ends go?

Function	Domain	Range	End Behavior
$f(x) = x^2$			As $x \rightarrow +\infty$, $f(x) \rightarrow$ <input type="text"/> . As $x \rightarrow -\infty$, $f(x) \rightarrow$ <input type="text"/> .
$f(x) = x^4$			As $x \rightarrow +\infty$, $f(x) \rightarrow$ <input type="text"/> . As $x \rightarrow -\infty$, $f(x) \rightarrow$ <input type="text"/> .
$f(x) = x^6$			As $x \rightarrow +\infty$, $f(x) \rightarrow$ <input type="text"/> . As $x \rightarrow -\infty$, $f(x) \rightarrow$ <input type="text"/> .

Does it change if I have a negative coefficient? How?

End Behavior

Using a graphing calculator find the end behavior of the following functions. Where do the ends go?

Function	Domain	Range	End Behavior
$f(x) = x$			As $x \rightarrow +\infty$, $f(x) \rightarrow$ <input type="text"/> . As $x \rightarrow -\infty$, $f(x) \rightarrow$ <input type="text"/> .
$f(x) = x^3$			As $x \rightarrow +\infty$, $f(x) \rightarrow$ <input type="text"/> . As $x \rightarrow -\infty$, $f(x) \rightarrow$ <input type="text"/> .
$f(x) = x^5$			As $x \rightarrow +\infty$, $f(x) \rightarrow$ <input type="text"/> . As $x \rightarrow -\infty$, $f(x) \rightarrow$ <input type="text"/> .

Does it change if I have a negative coefficient? How?

Multiplicity

The **power** of the factor determines the nature of the intersection at the point $x = a$.
(This is referred to as the **multiplicity**.)

Straight intersection:

$(x - a)^1$ The power of the zero is 1.

Tangent intersection :

$(x - a)^{\text{even}}$ The power of the zero is even.

Inflection intersection: (like a slide through)

$(x - a)^{\text{odd}}$ The power of the zero is odd.

Graph on a calculator and state the factors, zeros, multiplicity at each zero, extrema

$$f(x) = x^3$$

$$f(x) = x^2(x - 2)$$

$$f(x) = x(x - 2)(x + 2)$$

Graph the function

$$g(x) = -(x-4)(x-1)(x+1)(x+2)$$

Write a function in intercept form for the given graphs whose intercepts are integers. Assume the constant factor of a is either 1 or -1 .



