

6-3 Factoring Polynomials

Remember the factoring patterns you already know:

Difference of two squares: $a^2 - b^2 = (a - b)(a + b)$

Perfect square trinomials: $a^2 + 2ab + b^2 = (a + b)^2$

$$a^2 - 2ab + b^2 = (a - b)^2$$

There are two other factoring patterns that will prove useful:

Sum of two cubes: $a^3 + b^3 = (a + b)(a^2 - ab + b^2)$

Difference of two cubes: $a^3 - b^3 = (a - b)(a^2 + ab + b^2)$

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Ⓐ $x^3 + x^2 + x + 1$

Write out the polynomial.

$$x^3 - x^2 + x - 1$$

Group by common factor.

$$(x^3 - x^2) + (x - 1)$$

Factor.

$$x^2(x - 1) + 1(x - 1)$$

Regroup.

$$(x^2 + 1)(x - 1)$$

Ⓑ $x^4 + x^3 + x + 1$

Factor.

$$3x^3 + 7x^2 + 4x$$

$$4a^4b + 8a^3b^3 - 10a^2b^4$$