## 3-4 Graphing Logarithmic Functions

> Logarithms \& Exponentials
$f(x)=2^{x} \& f(x)=\log _{2} x$ are inverses

$x=2^{y} \quad$ 1. switch $x \& y$
$y=\log _{2} x$ 2. solve for $y$
natural log

$$
f(x)=\ln x
$$



Complete the table for the function $f(x)=\log x$
Then plot the points on the graph and connect the dots.

| $x$ | $f(x)=\log x$ |
| :---: | :---: |
| 0.1 |  |
| 1 |  |
| 10 |  |



Complete the table for the function $f(x)=\ln x$
Then plot the points on the graph and connect the dots.

| $x$ | $f(x)=\ln x$ |
| :---: | :---: |
| $\frac{1}{e} \approx 0.368$ |  |
| 1 |  |
| $e \approx 2.72$ |  |
| $e^{2} \approx 7.39$ |  |



Describe the transformations on each graph:
$f(x)=\log (x+2)$
$f(x)=3 \log (-x)-4$
$f(x)=-2 \ln (2 x)+5$

Analyze the graphs of:

$$
f(x)=\log x
$$

$$
f(x)=\ln x
$$

Domain:

Range:

End
behavior:

VA/HA:

Increasing/
Decreasing:

Intercepts:

## Graphing Transformed Logarithmic Functions

When graphing a transformed function, it is helpful to consider the following features of the graph: the vertical asymptote, and two reference points $(1,0)$ and (b,1).

| Function | $\boldsymbol{f}(\boldsymbol{x})=\log _{\mathbf{b}} \boldsymbol{x}$ | $\boldsymbol{g}(\boldsymbol{x})=\boldsymbol{a} \log _{\mathbf{b}}(\boldsymbol{x}-\boldsymbol{h})+\boldsymbol{k}$ |
| :--- | :---: | :---: |
| Asymptote | $x=0$ | $x=h$ |
| Reference point | $(1,0)$ | $(1+h, k)$ |
| Reference point | $(b, 1)$ | $(b+h, a+k)$ |

Graph and analyze the following functions:

| $f(x)=2 \cdot \log (x-1)$ |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 4 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |
| Domain: | 2 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  | $x$ |
| Range: | 0 | 2 | 4 | 6 |  | 8 | 10 |  |
|  | -2 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |
|  | $-^{-4}$ |  |  |  |  |  |  |  |

$f(x)=\log _{2}(x+1)-3$
Domain:

Range:

End
behavior:

End

VA/HA:
VA/HA:

| Increasing/ | Increasing/ |
| :--- | :--- |
| Decreasing: | Decreasing: |

## Intercepts:

Intercepts:

$$
f(x)=3 \cdot \ln (x)+2
$$

## Domain:

Range:

End

behavior:

## VA/HA:

## Increasing/

Decreasing:

Intercepts:

